

## Projects

**Project 1.** *The Dowry problem:* (Problem 47 in [Mos87]).

**Project 2.** *Euler's pentagonal theorem:* (Theorem 4 in [AE04]).

**Project 3.** *Generating function of Catalan's numbers:* (Proposition 1.3.1 in [Sta15]).

**Project 4.** *Egg droping numbers:* ([Boa04]).

**Project 5.** *Eigenvalues and walks on graphs:* (Chapter 1 of [BH12]).

**Project 6.** *Matrix Tree theorem:* (Chapter 4 of [Bap14]).

**Project 7.** *Chromatic polynomial:* (Chapter 1 of [BS18]).

**Project 8.** *Euler's formula and its applications:* ([Ric19]).

**Project 9.** *Sperner's lemma:* (Chapter 4 of [Sha91]).

**Project 10.** *Game of Hex:* (Chapter 9 of [DK16]).

**Project 11.** *Bernoulli numbers and sum of powers:* (Chapter 2.2 of [You92]).

**Project 12.** *Eulerian numbers:* (Chapter 1 of [Pet15]).

**Project 13.** *Josephus problem:* (Chapter 1 of [GKP94]).

**Project 14.** *Unravelling Knots:* (Chapter 5 of [Pra00]).

**Project 15.** *Arrow's theorem in Voting theory:* (Chapter 4 of [HK18]).

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